

# TEHNIČKA MEHANIKA

Inženjerstvo zaštite životne sredine

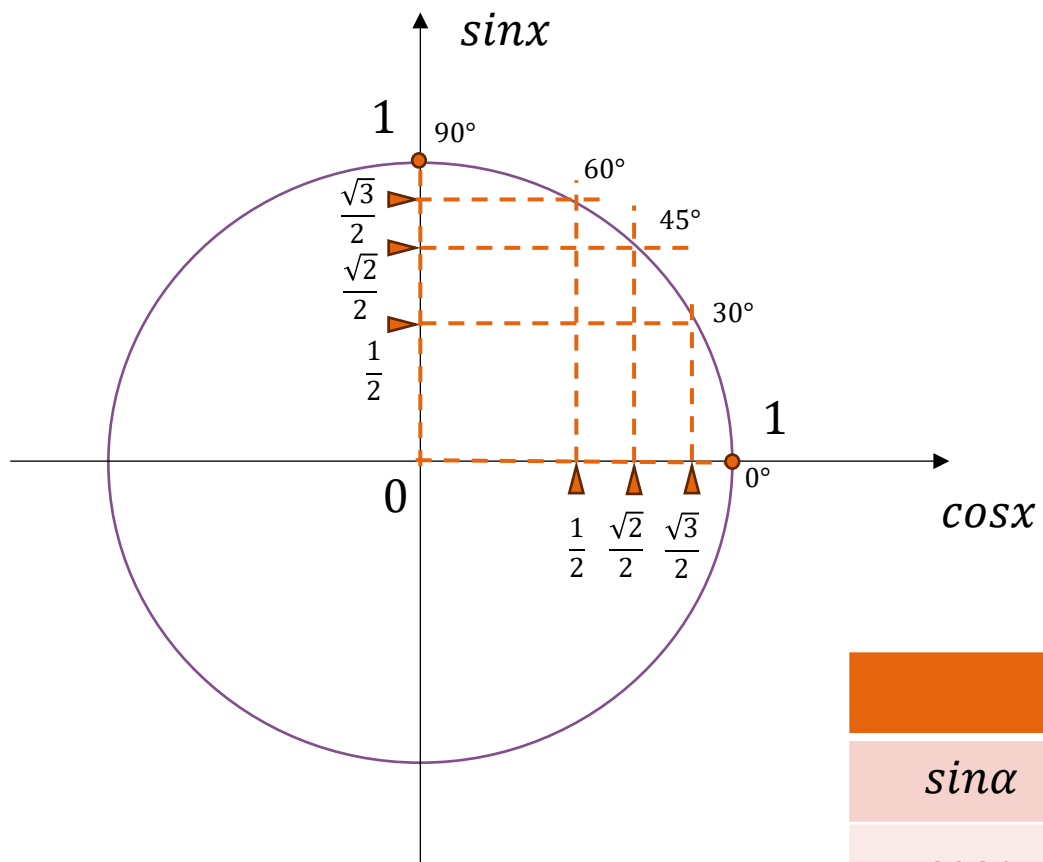
Asistent:

Gordana Jović

Profesor:

Boban Cvetanović

# TRIGONOMETRIJSKI KRUG



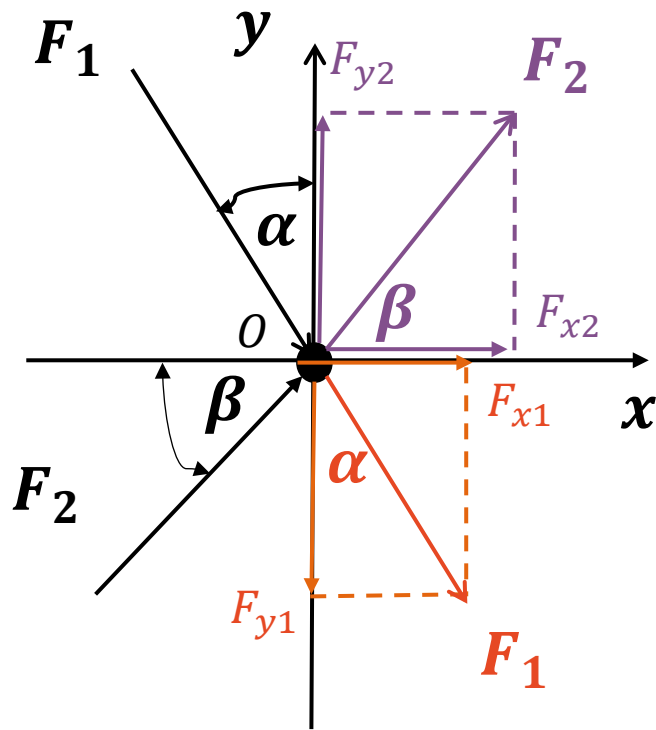
|               | $0^\circ$ | $30^\circ$           | $45^\circ$           | $60^\circ$           | $90^\circ$ |
|---------------|-----------|----------------------|----------------------|----------------------|------------|
| $\sin \alpha$ | 0         | $\frac{1}{2}$        | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{3}}{2}$ | 1          |
| $\cos \alpha$ | 1         | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{1}{2}$        | 0          |

# PROJEKCIJA SILE NA X I Y OSU

## ZADATAK 4.

Izračunati intenzitete komponenti sila  $F_1$  i  $F_2$ , ako je  $F_1 = 12\text{N}$ ,  $F_2 = 8\text{N}$ ,  $\alpha = 30^\circ$ ,  $\beta = 60^\circ$ .

$$F_{x1} = ? ; F_{y1} = ? ; F_{x2} = ? ; F_{y2} = ?$$



$$\sin\alpha = \frac{F_{1x}}{F_1}$$

$$F_{x1} = F_1 * \sin\alpha$$

$$F_{x1} = 12 * \sin 30^\circ$$

$$F_{x1} = 12 * \frac{1}{2}$$

$$F_{x1} = 6\text{ N}$$

$$\cos\alpha = \frac{F_{1y}}{F_1}$$

$$F_{y1} = F_1 * \cos\alpha$$

$$F_{y1} = 12 * \cos 30^\circ$$

$$F_{y1} = 12 * \frac{\sqrt{3}}{2}$$

$$F_{y1} = 6\sqrt{3}\text{ N}$$

$$F_{x2} = F_2 * \cos\beta$$

$$F_{x2} = 8 * \cos 60^\circ$$

$$F_{x2} = 8 * \frac{1}{2}$$

$$F_{x2} = 4\text{ N}$$

$$F_{y2} = F_2 * \sin\beta$$

$$F_{y2} = 8 * \sin 60^\circ$$

$$F_{y2} = 8 * \frac{\sqrt{3}}{2}$$

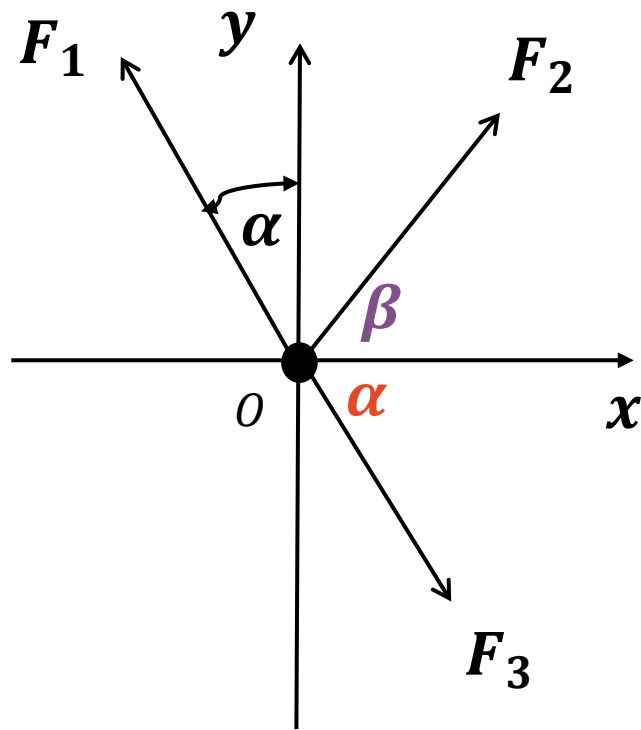
$$F_{y2} = 4\sqrt{3}\text{ N}$$

# PROJEKCIJA SILE NA X I Y OSU

## ZADATAK 5.

Izračunati intenzitete komponenti sila  $F_1$  i  $F_2$ , ako je  $F_1 = 20\text{N}$ ,  $F_2 = 8\text{N}$ ,  $F_3 = 9\text{N}$ ,  $\alpha = 30^\circ$ ,  $\beta = 60^\circ$ .

$$F_{x1} = ? ; F_{y1} = ? ; F_{x2} = ? ; F_{y2} = ? ; F_{x3} = ? ; F_{y3} = ?$$



REŠENJE:

$$F_{x1} = 10 \text{ N}$$

$$F_{y2} = 4\sqrt{3} \text{ N}$$

$$F_{y1} = 10\sqrt{3} \text{ N}$$

$$F_{x3} = 4.5\sqrt{3} \text{ N}$$

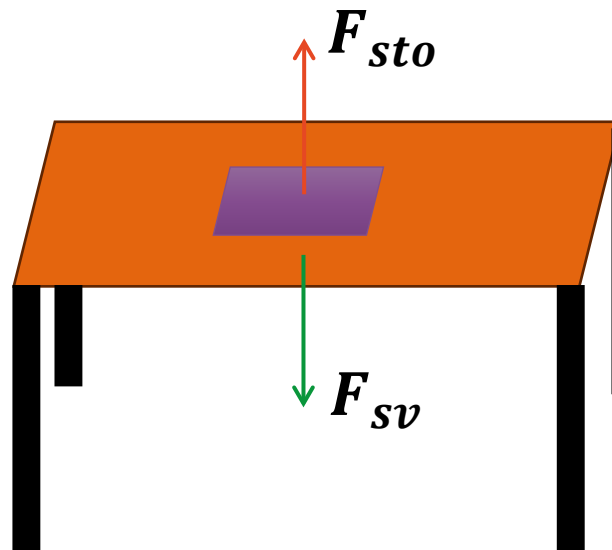
$$F_{x2} = 4 \text{ N}$$

$$F_{y3} = 4.5 \text{ N}$$

# VEZE I REAKCIJE VEZA

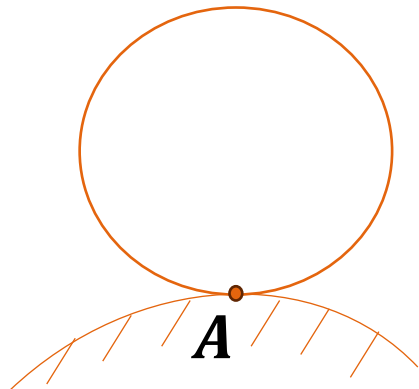
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*Svako telo čije je slobodno kretanje u prostoru ograničeno bilo kojim drugim telom, naziva se **VEZANO – NE SLOBODNO TELO***

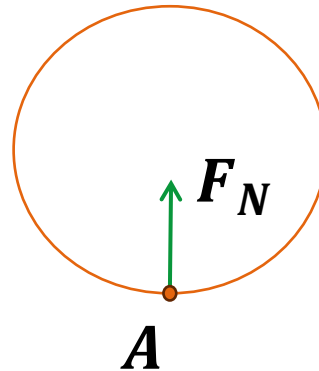


# GLATKE POVRŠI ILI OSLONAC

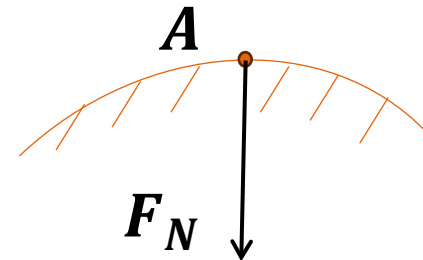
*Ako se može zanemariti trenje koje se javlja između dva tela koja se dodiruju.  
onda se takve površi smatraju **GLATKIM**.*



*REAKCIJA (podloga)  
dodiruje telo*

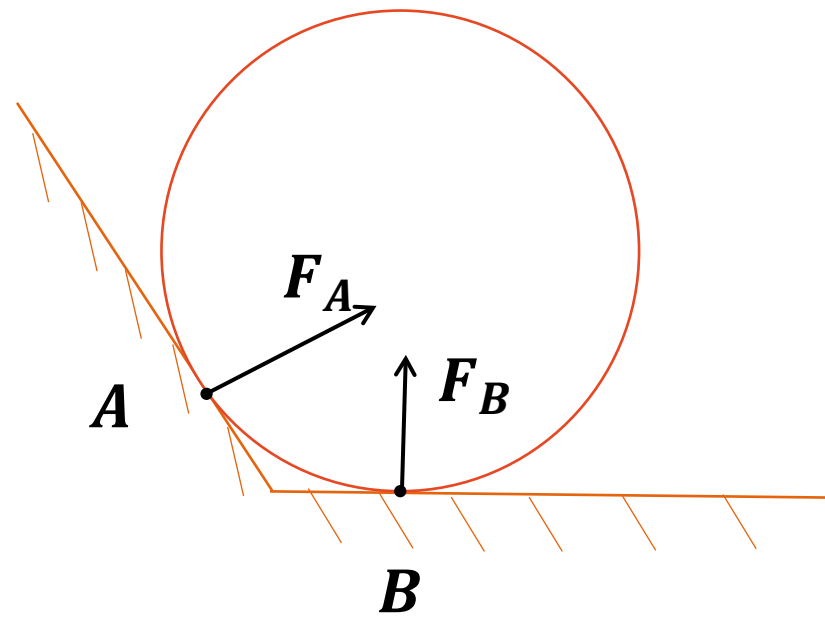
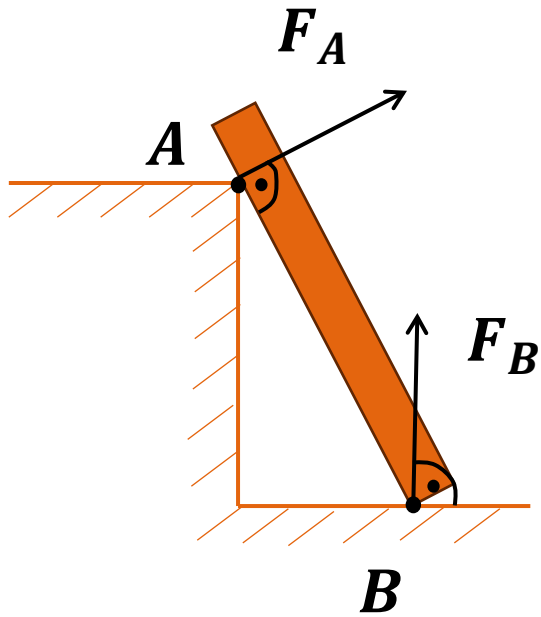


*telo dodiruje  
podlogu*



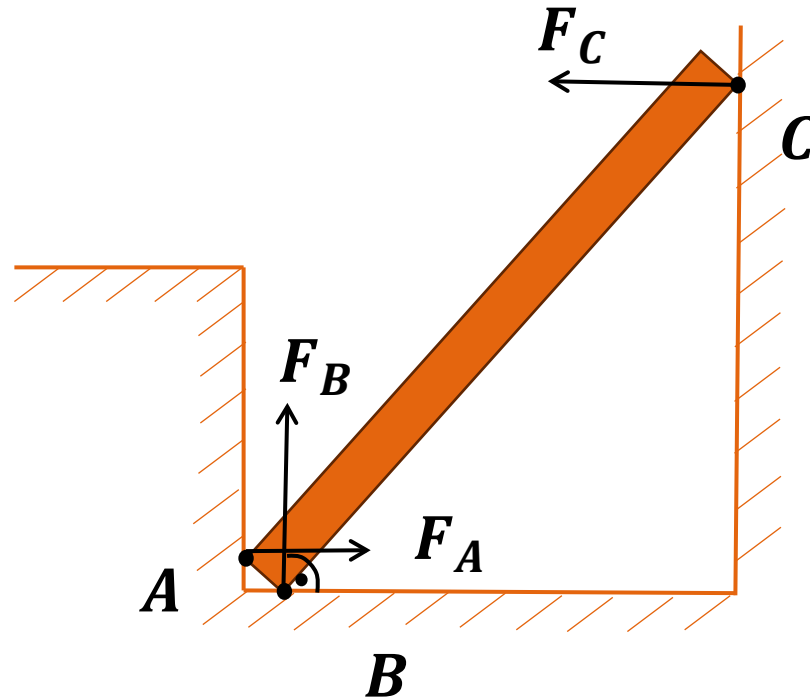
# GLATKE POVRŠI ILI OSLOONAC

*Kada jedna od dodirnih površi predstavlja tačku, onda reakcija veze leži na normalni druge površi.*



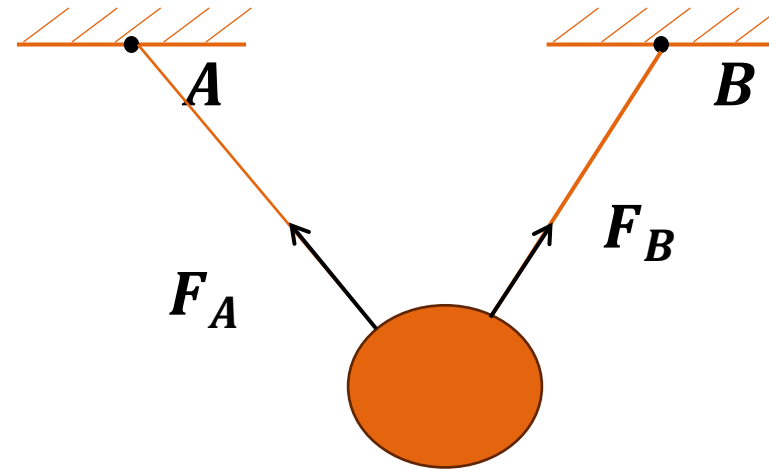
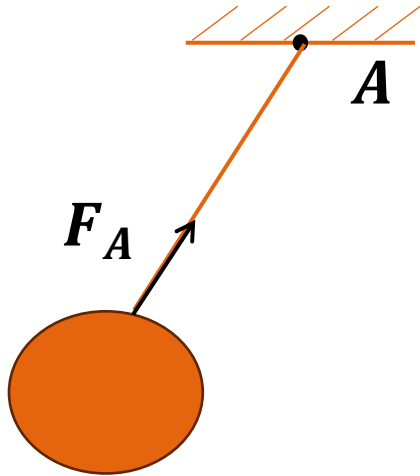
# GLATKE POVRŠI ILI OSLOONAC

*Ako se kruto telo svojim krajem oslanja na ugao, onda ugao sprečava pomeranje ovog kraja po horizontali ulevo ( $x$  – pravac) i vertikali naniže ( $y$  – pravac).*



# UŽE

*Veza ostvarena pomoću užeta, lanca, kaiša itd. nedozvoljavaju teretu da se idalje od tačke A.*

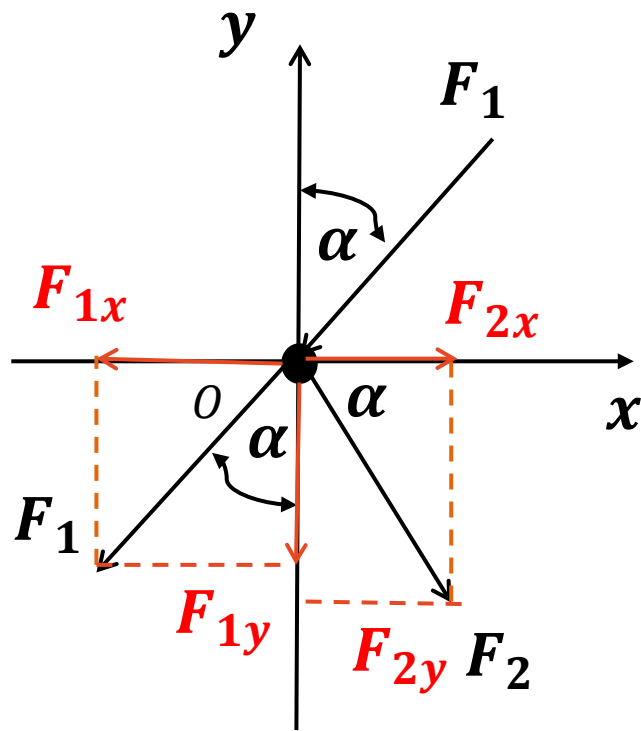


# PROJEKCIJA SILE NA X I Y OSU

## ZADATAK 1.

Izračunati intenzitete komponenti sila  $F_1$  i  $F_2$ , ako je  $F_1 = 4 \text{ kN}$ ,  $F_2 = 12 \text{ kN}$ ,  $\alpha = 60^\circ$ .

$$F_{x1} = ? ; F_{y1} = ? ; F_{x2} = ? ; F_{y2} = ?$$



REŠENJE:

$$F_{1x} = F_1 * \sin \alpha$$

$$F_{1x} = 4 * \sin 60^\circ$$

$$F_{1x} = 4 * \frac{\sqrt{3}}{2}$$

$$F_{1x} = 2\sqrt{3} \text{ kN}$$

$$F_{1y} = F_1 * \cos \alpha$$

$$F_{1y} = 4 * \cos 60^\circ$$

$$F_{1y} = 4 * \frac{1}{2}$$

$$F_{1y} = 2 \text{ kN}$$

$$F_{2x} = F_2 * \cos \alpha$$

$$F_{2x} = 12 * \cos 60^\circ$$

$$F_{2x} = 12 * \frac{1}{2}$$

$$F_{2x} = 6 \text{ kN}$$

$$F_{2y} = F_2 * \sin \alpha$$

$$F_{2y} = 12 * \sin 60^\circ$$

$$F_{2y} = 12 * \frac{\sqrt{3}}{2}$$

$$F_{2y} = 6\sqrt{3} \text{ kN}$$

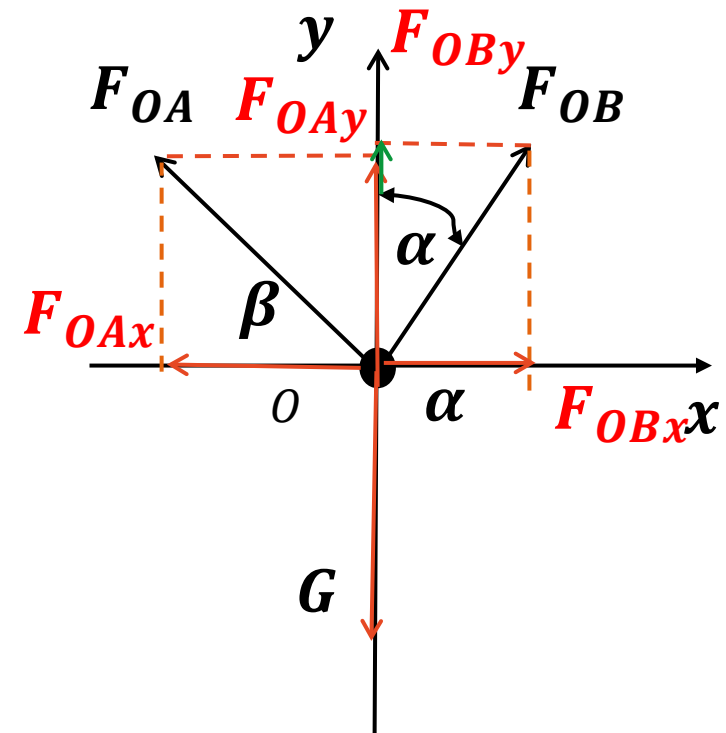
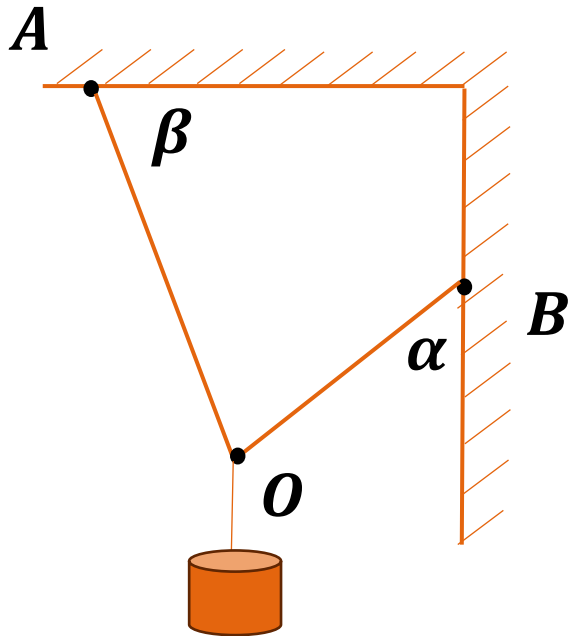
# PROJEKCIJA SILE NA X I Y OSU

## ZADATAK 2.

Izračunati intenzitete komponenti sila  $F_1$  i  $F_2$ , ako je  $F_{OB} = 20 \text{ kN}$ ,  $F_{OA} = 12 \text{ kN}$ ,  $\alpha = 45^\circ$ ,  $\beta = 60^\circ$ .

$$F_{x1} = ? ; F_{y1} = ? ; F_{x2} = ? ; F_{y2} = ?$$

REŠENJE:

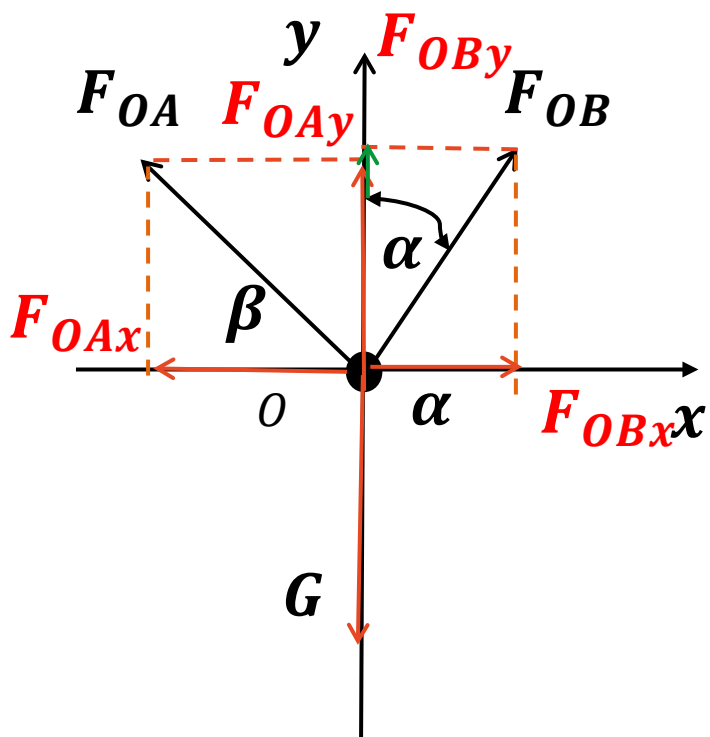


# PROJEKCIJA SILE NA X I Y OSU

## ZADATAK 2.

Izračunati intenzitete komponenti sila  $F_1$  i  $F_2$ , ako je  $F_{OB} = 20 \text{ kN}$ ,  $F_{OA} = 12 \text{ kN}$ ,  $\alpha = 45^\circ$ ,  $\beta = 60^\circ$ .

$$F_{x1} = ? ; F_{y1} = ? ; F_{x2} = ? ; F_{y2} = ?$$



REŠENJE:

$$F_{OAx} = F_{OA} * \cos\beta$$

$$F_{OAx} = 12 * \cos 60^\circ$$

$$F_{OAx} = 12 * \frac{1}{2}$$

$$F_{OAx} = 6 \text{ kN}$$

$$F_{OAy} = F_{OA} * \sin\beta$$

$$F_{OAy} = 12 * \sin 60^\circ$$

$$F_{OAy} = 12 * \frac{\sqrt{3}}{2}$$

$$F_{OAy} = 6\sqrt{3} \text{ kN}$$

$$F_{OBx} = F_{OB} * \sin\alpha \quad F_{OBy} = F_{OB} * \cos\alpha$$

$$F_{OBx} = 20 * \sin 45^\circ \quad F_{OBy} = 20 * \sin 45^\circ$$

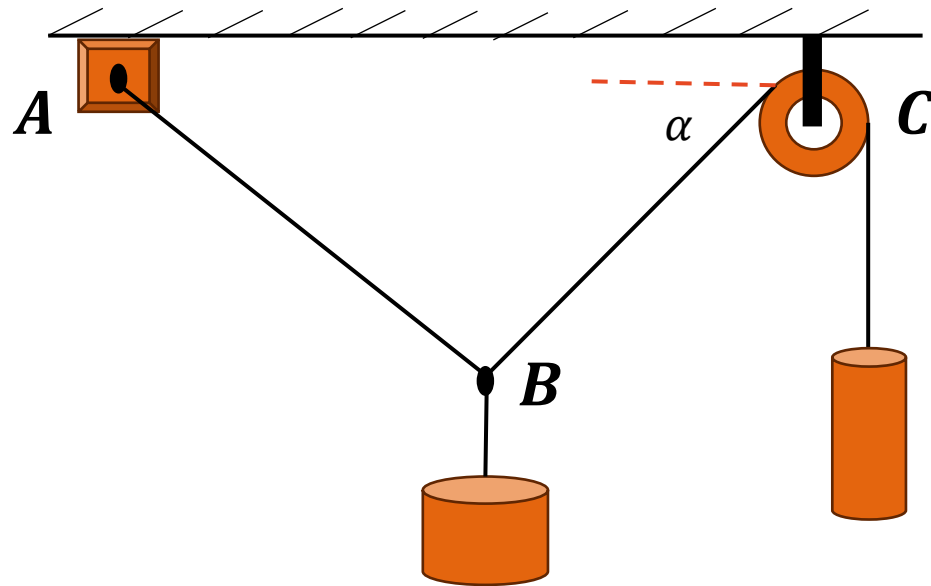
$$F_{OBx} = 20 * \frac{\sqrt{2}}{2} \quad F_{OBy} = 20 * \frac{\sqrt{2}}{2}$$

$$F_{OBx} = 10\sqrt{2} \text{ kN}$$

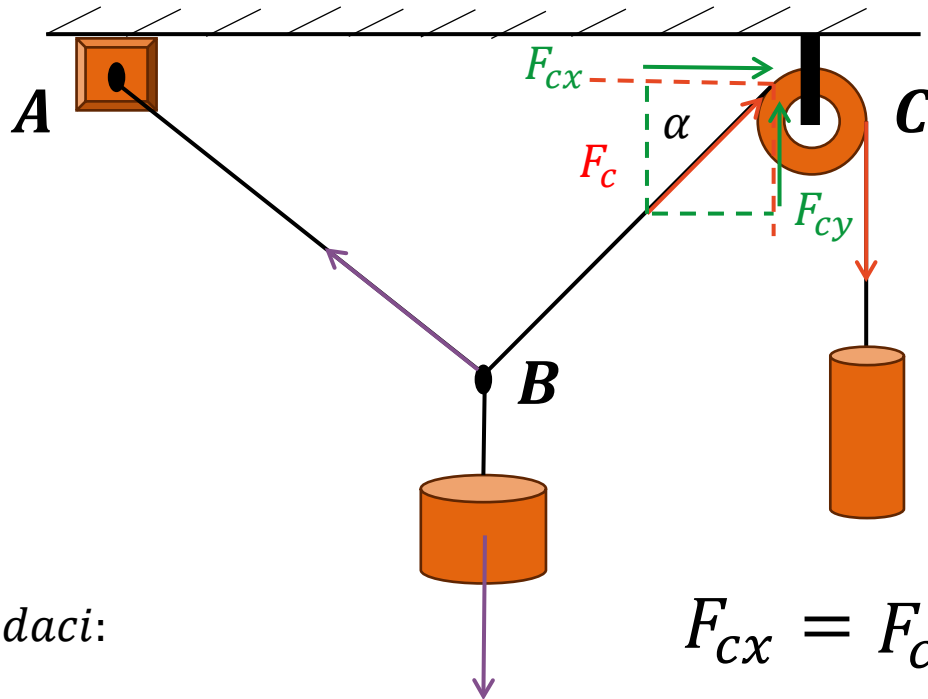
$$F_{OBy} = 10\sqrt{2} \text{ kN}$$

## ZADATAK 3.

- Za sistem prikazan na slici, potrebno je odrediti komponente sile u užetu BC. Ako je težina tela u tački B  $=30\text{kg}$  a u tački C  $=78\text{kg}$ , ugao  $\alpha = 30^\circ$ .



# ZADATAK 3.



$$F_c = m_c * a \rightarrow a = g = 9.81 \frac{m}{s^2}$$

$$F_c = 78 * 9.81$$

$$F_c = 765.18 \text{ N}$$

Podaci:

$$m_b = 30 \text{ kg}$$

$$m_c = 78 \text{ kg}$$

$$\alpha = 30^\circ$$

$$F_{cx} = ? \quad F_{cy} = ?$$

$$F_{cx} = F_c * \cos \alpha$$

$$F_{cx} = 765.18 * \cos 30$$

$$F_{cx} = 662.665 \text{ N}$$

$$F_{cy} = F_c * \sin \alpha$$

$$F_{cy} = 765.18 * \sin 30$$

$$F_{cy} = 382.59 \text{ N}$$

HVALA NA PAŽNJI!

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PITANJA?